



# A Reliable Travel Time Prediction System with Sparsely Distributed Detectors

## Ph.D. Dissertation Proposal

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# Outline

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- Introduction
- Research Objectives
- Framework of the Travel Time Prediction System
- Travel Time Estimation Module
  - Existing models
  - The proposed hybrid model
- Travel Time Prediction
  - Existing models
  - The proposed hybrid model
- Summary
- On-going Works





# Introduction

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- Travel times (**completed** and **en-route trips**) are crucial information for an Advanced Traveler Information System (ATIS)
- Travel time prediction is a challenging task due to the impacts of
  - Geometric features
  - Traffic patterns
  - Availability of detection system, and
  - Nonrecurrent congestion (for example, incidents), etc.





# Introduction (cont' d)

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- Issues Associated with Existing Models and Systems:
  - High system costs
    - Densely distributed detectors (i.e., 0.5-mile apart)
    - Accurate speed detection
    - Recurrent measurement on travel times
      - Coifman et al. (2002, 2003), van Lint et al. (2003), Liu et al. (2006)
  - Reliability
    - Missing or delayed data
    - Nonrecurrent congestions (for example, incidents)





# Features of A Cost-efficient and Reliable Travel Time Prediction System

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- Required input variables should be obtainable from **sparsely distributed** traffic detectors
- Take advantage of some actual travel times from the field, but not rely on a large number of such data.
- Be capable of operating under **non-recurrent congestion** or **data-missing** conditions and effectively dealing with related issues during real-time operations.





# Research Objectives

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- Develop a travel time estimation module
  - Reliable estimates of completed trips
  - Under all types of recurrent traffic patterns
  - With sparsely distributed traffic detectors
- Construct a travel time prediction module
  - For freeway segments
  - Large detector spacing
  - Historical travel times and traffic patterns





# Research Objectives (cont' d)

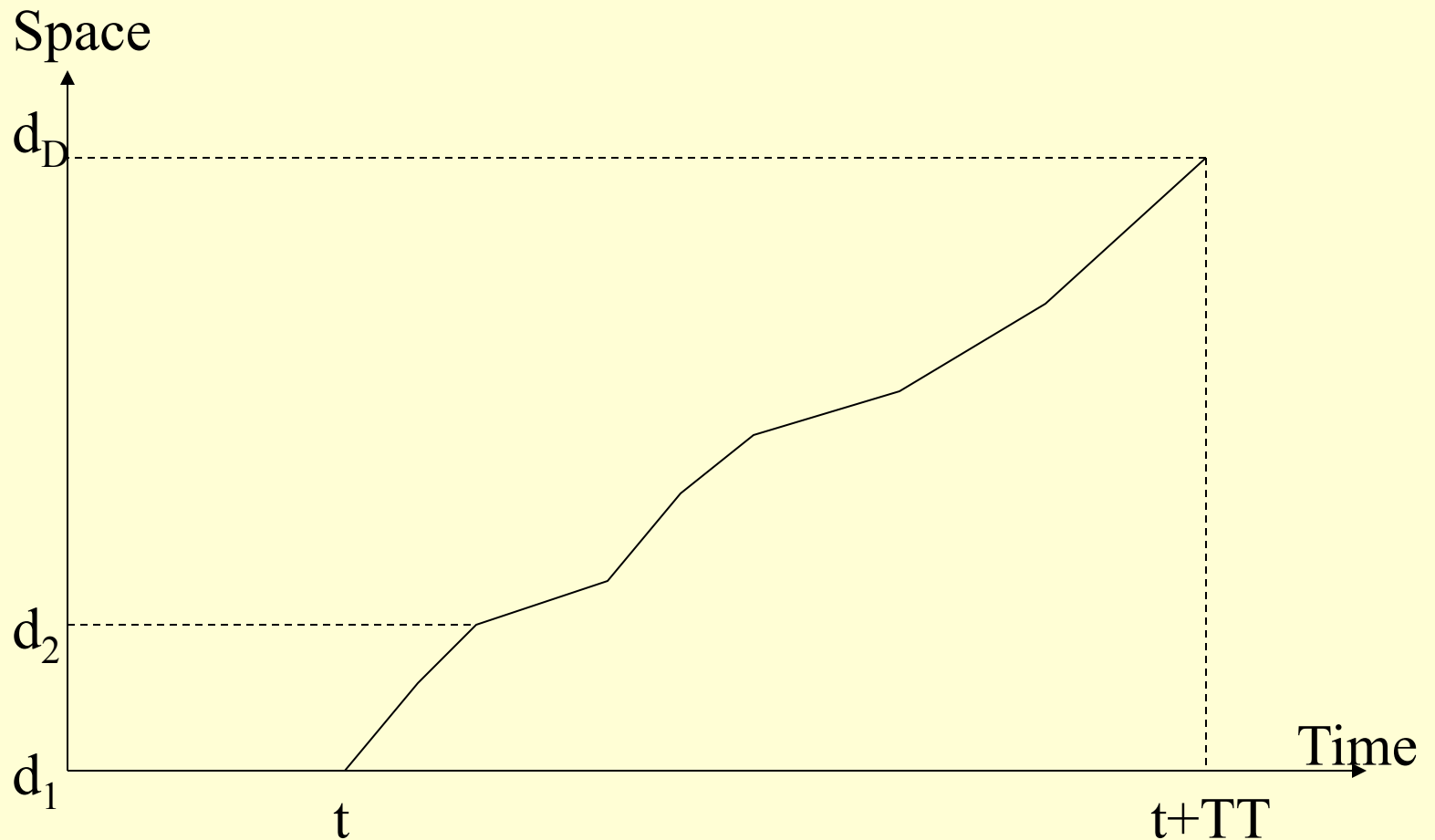
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- Integrate a missing data estimation module
  - To deal with various missing data and delay patterns
- Calibrate an incident detection module
  - Switch the travel time prediction system to a different mode (i.e., display delay warnings instead of predicted travel times) when an incident has been detected.





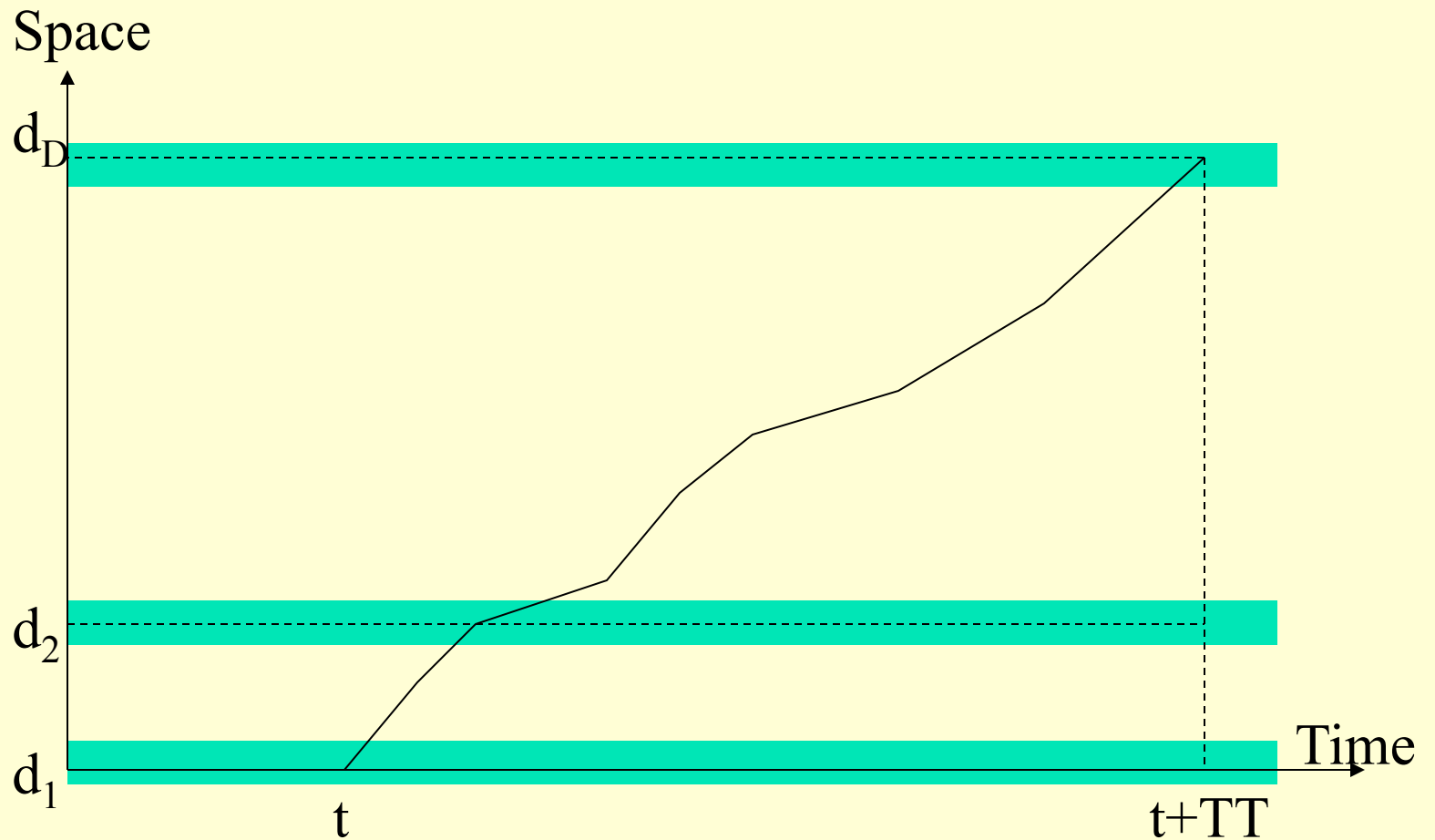
# T.T. Estimation vs. Prediction





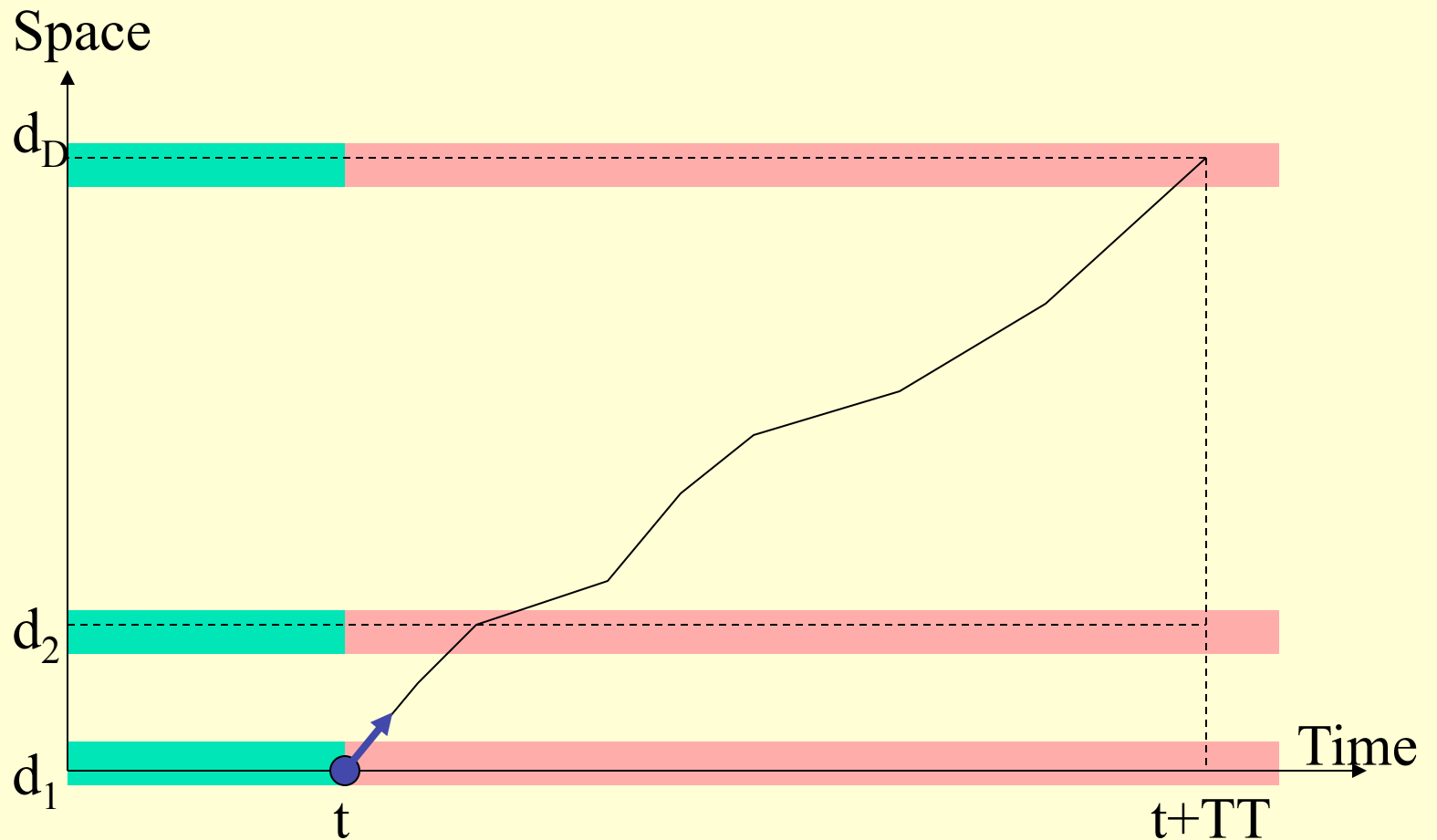


# T.T. Estimation





# T.T. Prediction





# Existing Travel Time Prediction Systems

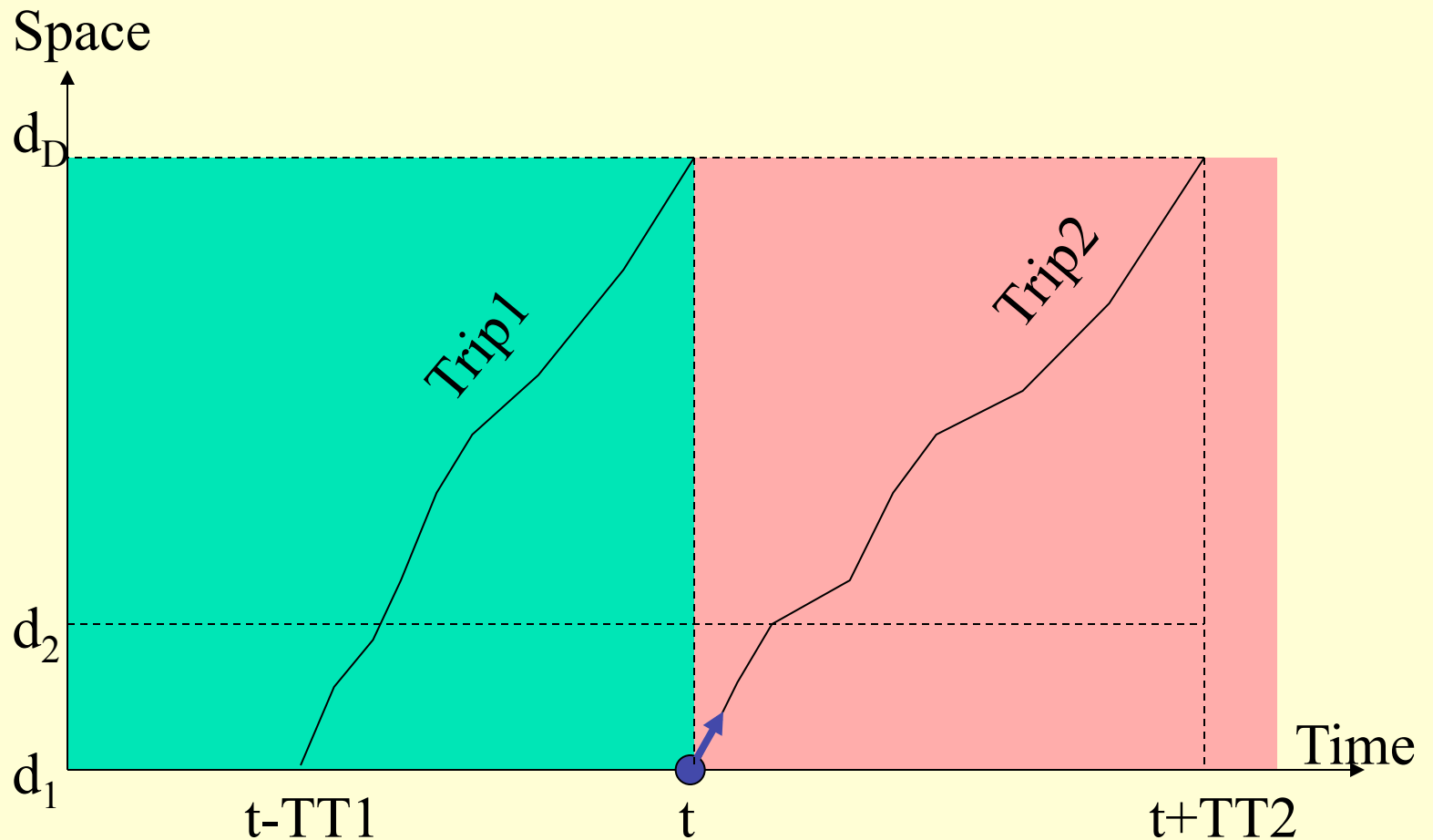
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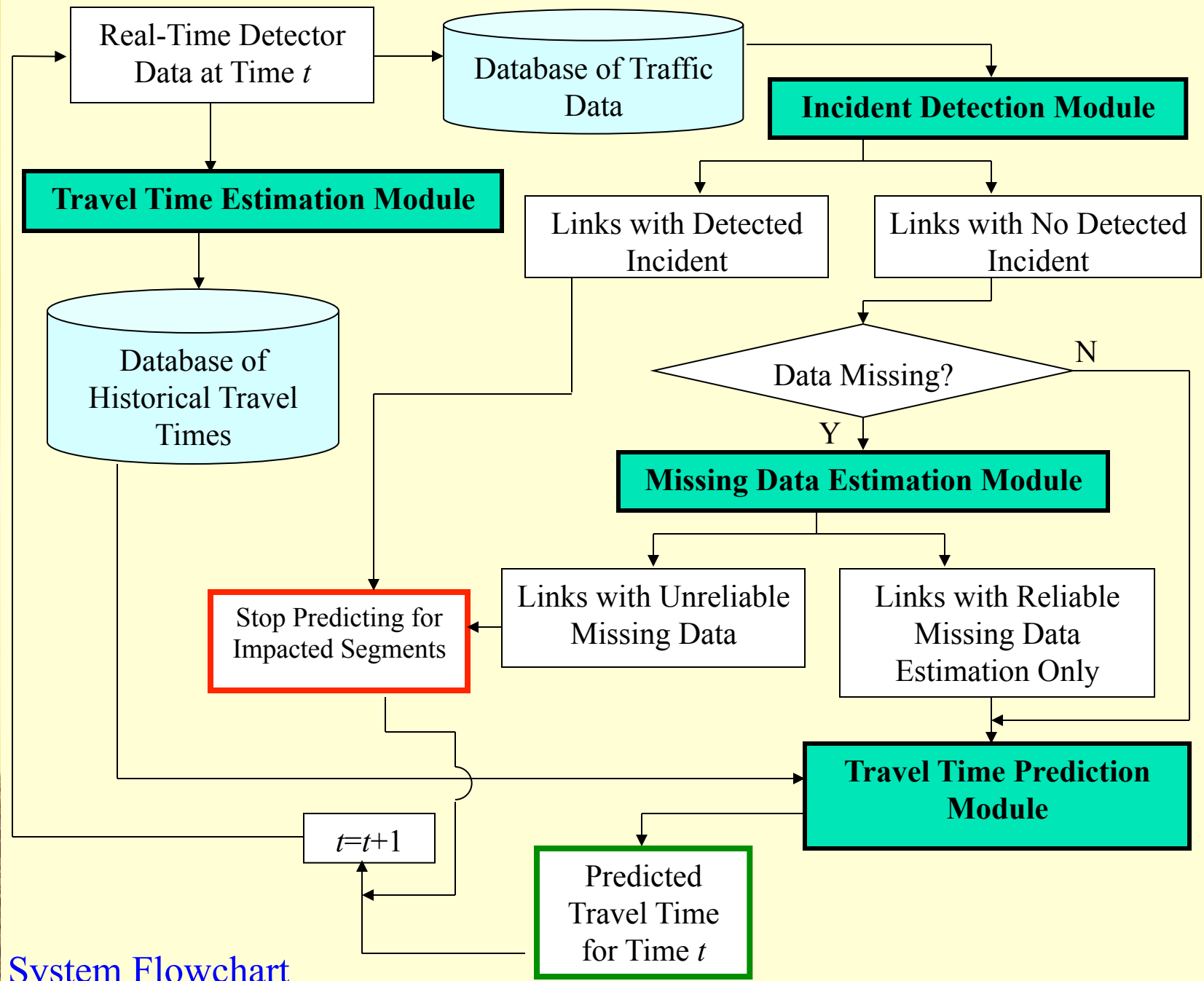
- Example systems
  - Houston, TX; Atlanta, GA; Chicago, IL; and Seattle, WA, etc.
- Almost all real-world systems use **current detected traffic conditions** as the prediction of the future
  - Completed trips instead of en-route trips
  - Big difference





# Completed Trips vs. En-route Trips





System Flowchart





# Literature Review

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- Travel Time Estimation
  - Flow-based models
  - Vehicle identification approaches
  - Trajectory-based models





# Limitations of Flow-based Models

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- Reliability of detector data
  - Detection errors (volume drifting) vary over time and space
- Traffic patterns
  - Require uniformly distributed traffic across all lanes
- Geometric features
  - Cannot model ramp impact





# Limitations of Vehicle Identification Approach

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- Traffic patterns
  - Lane-based approach, therefore requires low lane changing rate
  - Requires uniform traffic conditions across lanes
- Geometric features
  - May not fit geometric changes, such as lane drop and lane addition
- System cost
  - High. Require new hardware or high bandwidth
- Reliability
  - Low detection resolution under high speed
  - Reduced accuracy under low light (video-based)







# Limitations of Existing Trajectory-based Models

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- Assumes constant traffic-propagation speed
- May not perform well on long links
  - currently all studies are based on detectors less than 0.5-mile apart
- Requires reliable speed measurement
  - Not available from most traffic detectors





# A Hybrid Travel Time Estimation Model with Sparsely Distributed Detectors

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- A Clustered Linear Regression Model as the main model
  - For traffic scenarios that have sufficient field observations
- An Enhanced Trajectory-based Model as the supplemental model
  - For other scenarios





# Clustered Linear Regression Model

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- Travel times may be constrained in a range under one identified traffic scenario
  - For example, the travel time cannot be free-flow travel time when congestion is being observed at one detector
- Assume a linear relation between the travel time under one traffic scenario with traffic variables from pre-determined **critical lanes**



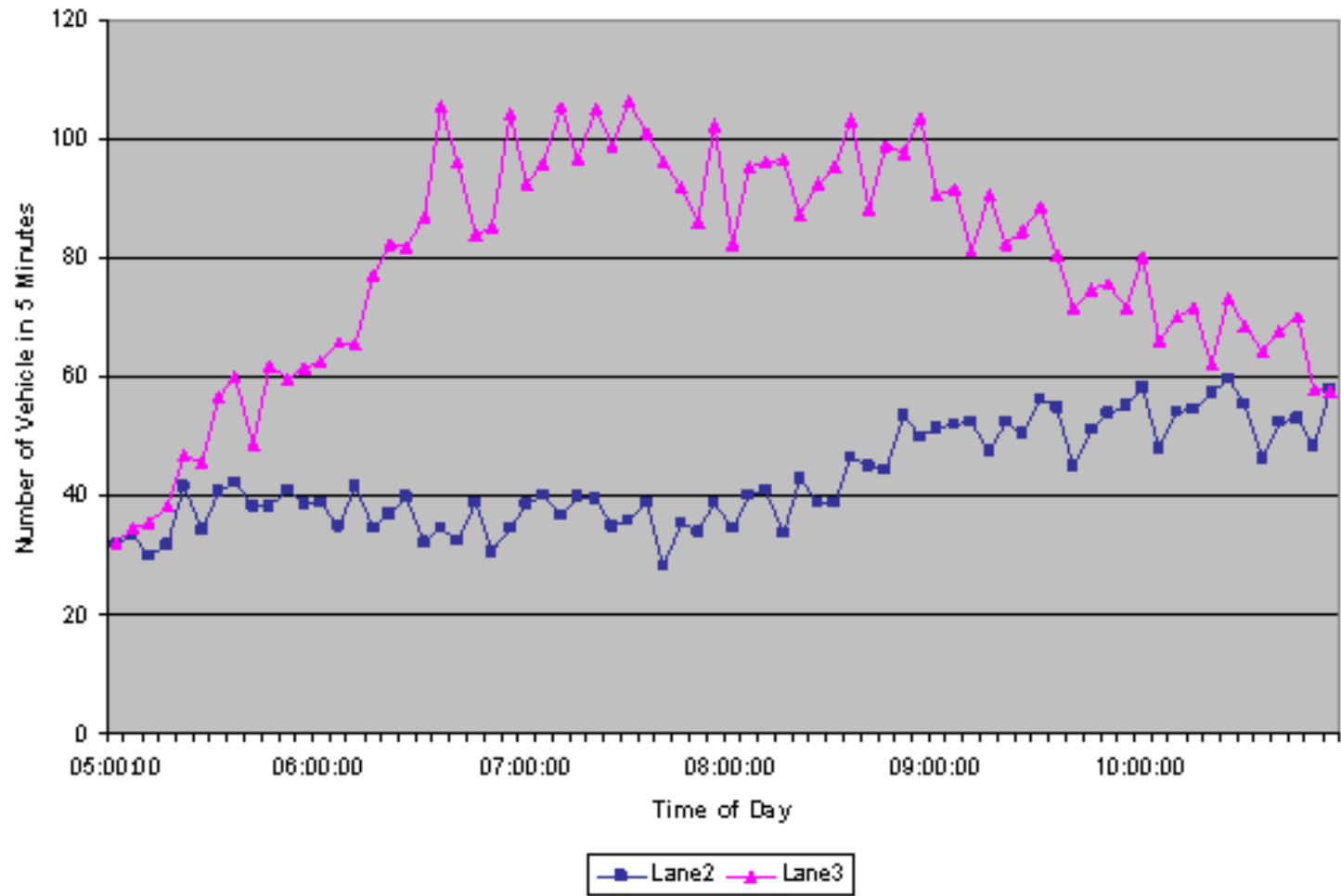
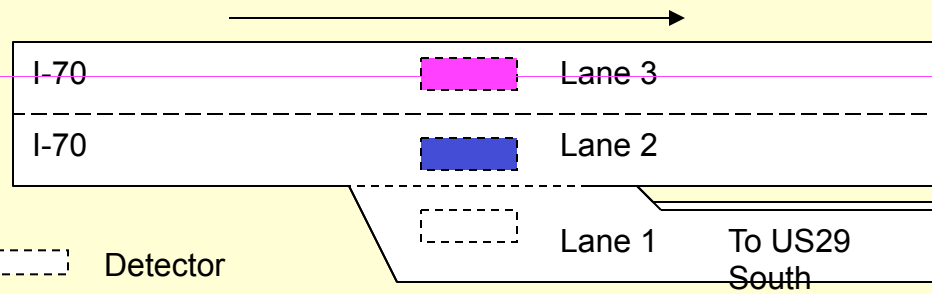


# Critical Lanes

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- Those lanes that directly contribute to estimate the average travel speed of through traffic
- May include both mainline lanes and ramp lanes
- From both upstream and downstream detector locations







# Model Formulation of the Clustered Linear Regression Model

$$\begin{aligned}\tau_d(t) = & \sum_{la \in \text{CLT}_{d,d+1}^a(p)} b_{d,la}^{T,p} \frac{o_{d,la}(t, \gamma_p^d \tau_d^E(p))}{v_{d,la}(t, \gamma_p^d \tau_d^E(p))} + \sum_{la \in \text{CLR}_{d,d+1}^a(p)} b_{d,la}^{R,p} \frac{o_{d,la}(t, \gamma_p^d \tau_d^E(p))}{v_{d,la}(t, \gamma_p^d \tau_d^E(p))} \\ & + \sum_{la \in \text{CLT}_{d,d+1}^{a+1}(p)} b_{d+1,la}^{T,p} \frac{o_{d,la}(t + \gamma_p^d \tau_d^E(p), (1 - \gamma_p^d) \tau_d^E(p))}{v_{d,la}(t + \gamma_p^d \tau_d^E(p), (1 - \gamma_p^d) \tau_d^E(p))} \\ & + \sum_{la \in \text{CLR}_{d,d+1}^{a+1}(p)} b_{d+1,la}^{R,p} \frac{o_{d,la}(t + \gamma_p^d \tau_d^E(p), (1 - \gamma_p^d) \tau_d^E(p))}{v_{d,la}(t + \gamma_p^d \tau_d^E(p), (1 - \gamma_p^d) \tau_d^E(p))} + b_d^{0,p}\end{aligned}$$





# An Enhanced Trajectory-based Model

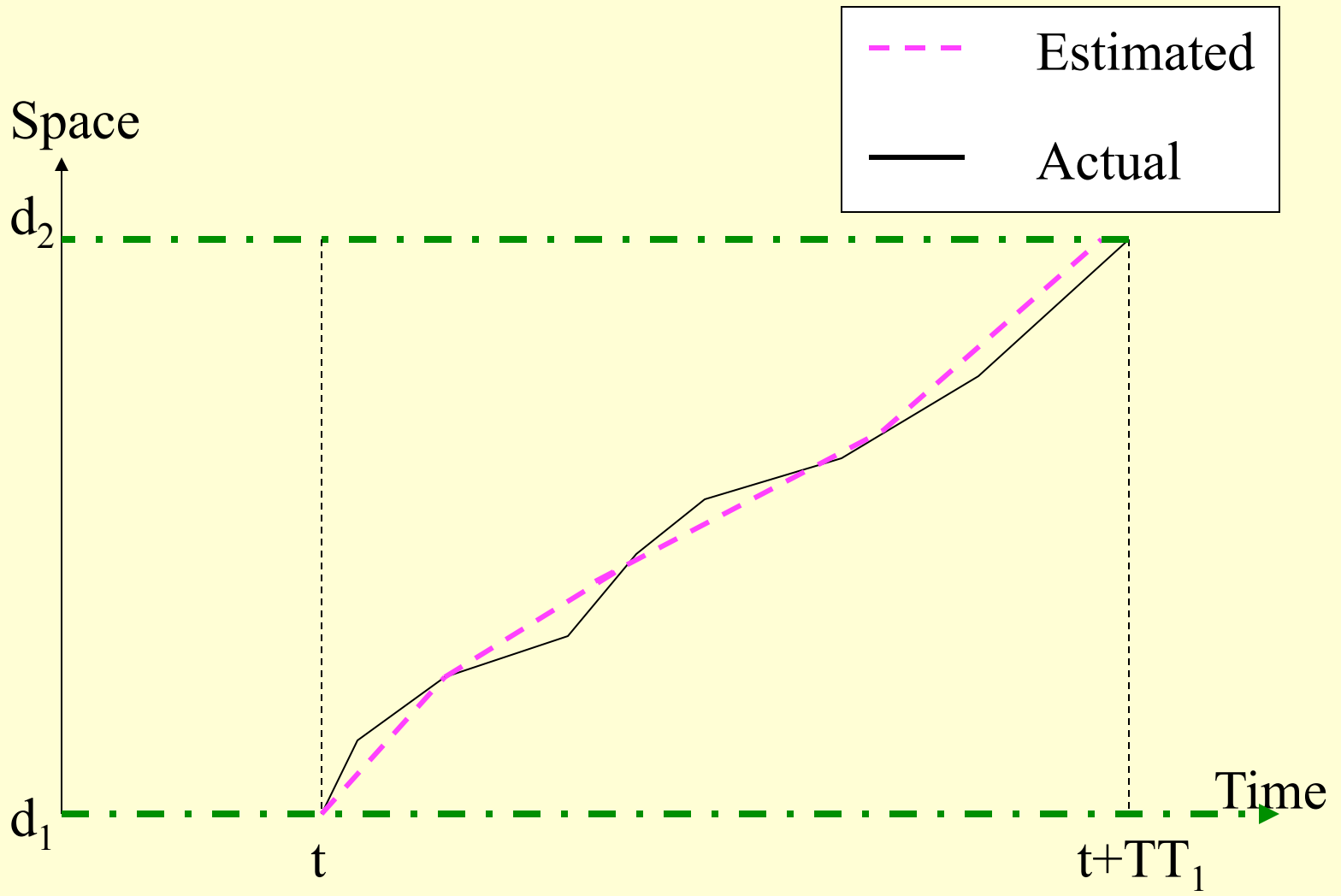
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- Combines and enhances two types of trajectory estimation:
  - Traffic propagation relations when the vehicle is close to one detector
  - An enhanced piecewise linear-speed-based model when the vehicle is far from both detectors
- Does not require speed in input variables
  - Estimate the occupancy first, then use occupancy-speed relation to estimate the vehicle's speed





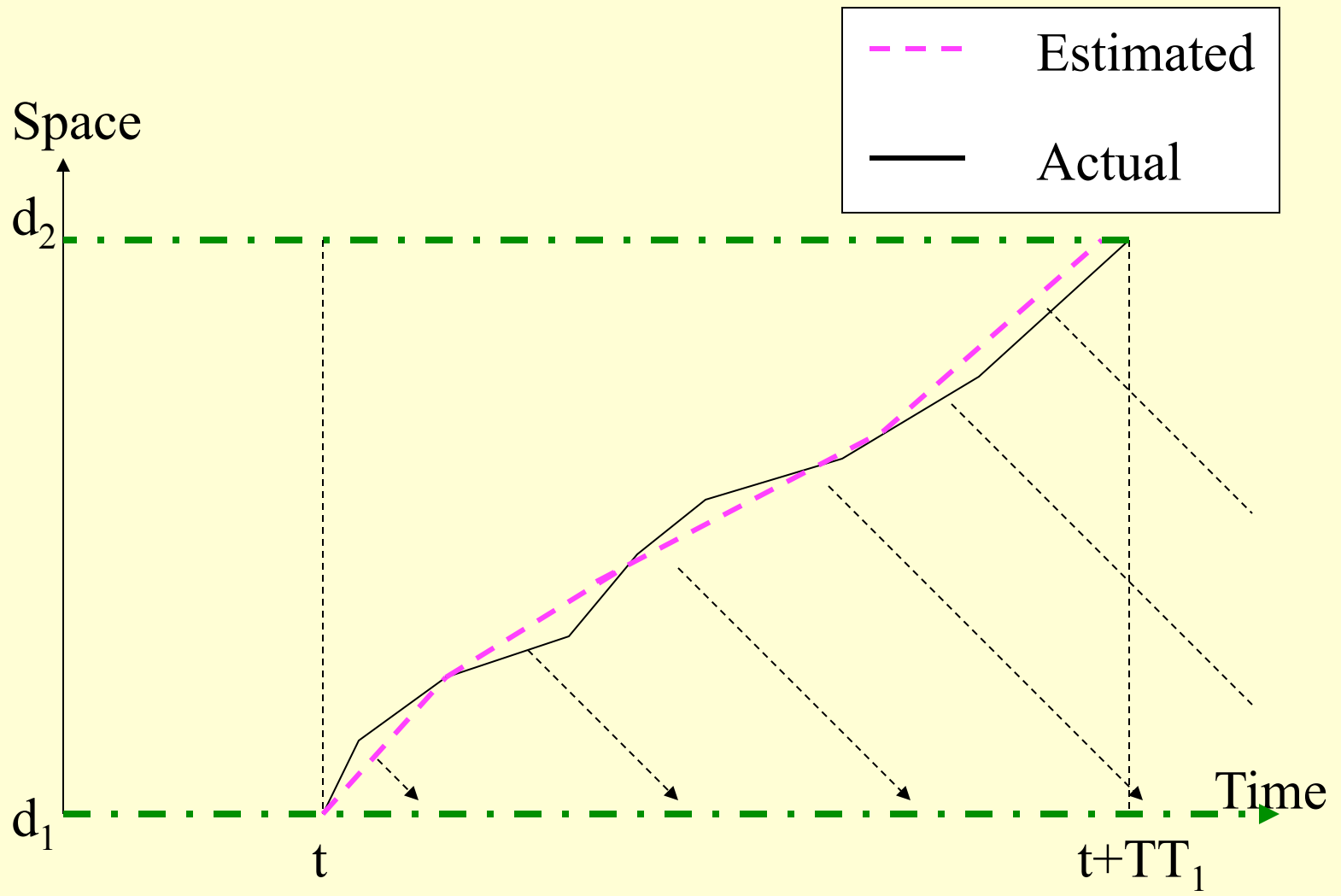
# Trajectory-based Method





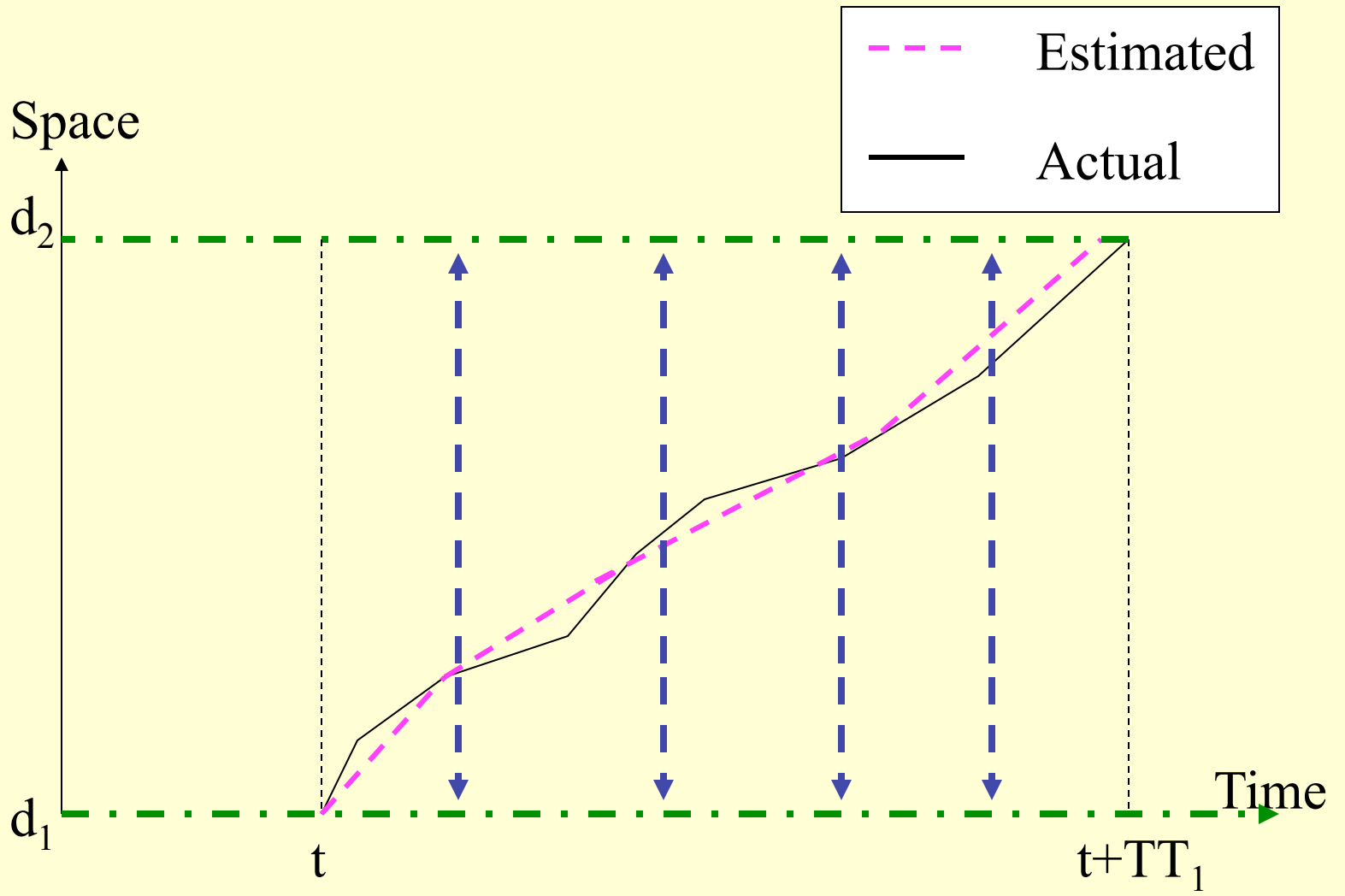


# Trajectory-based Method



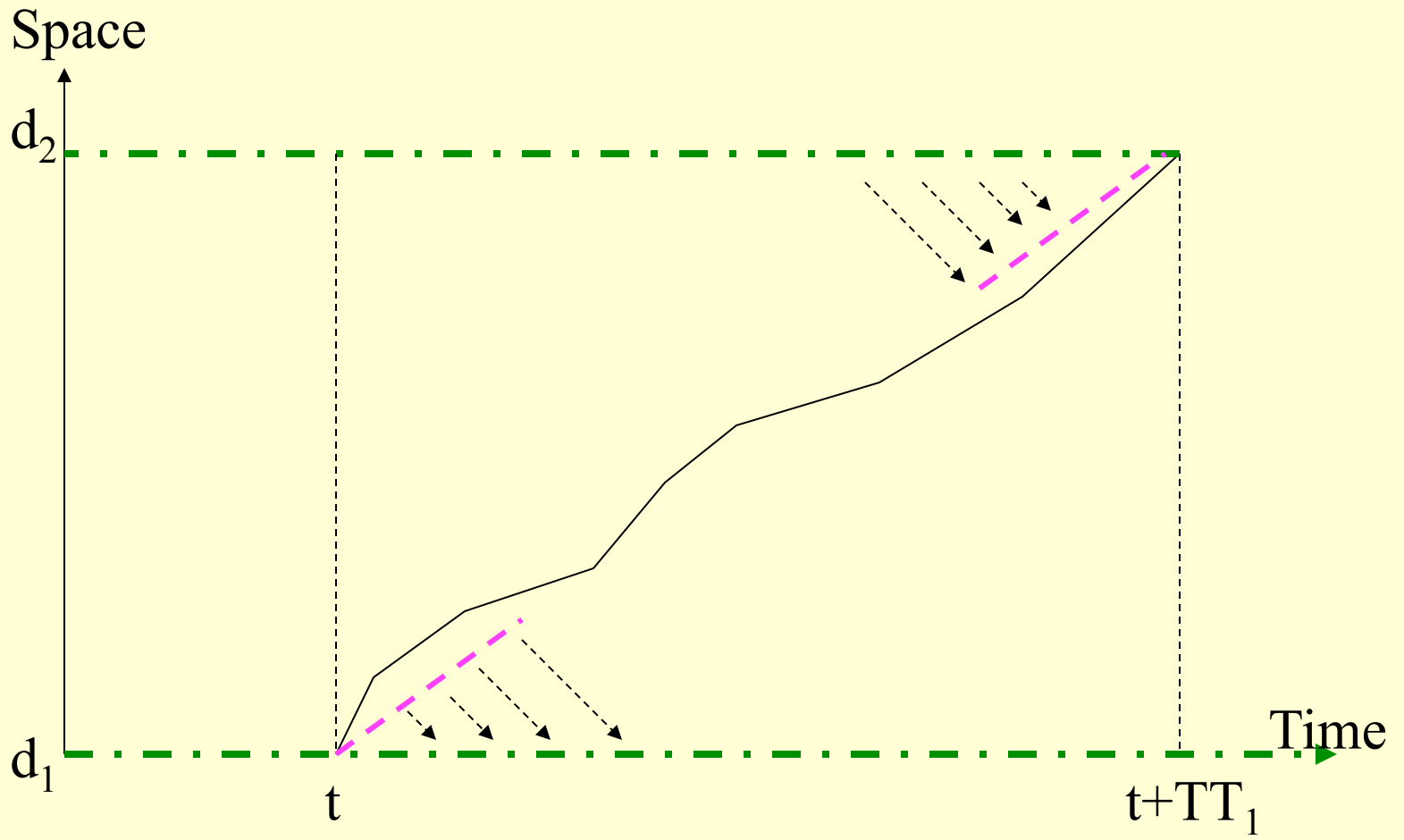


# Trajectory-based Method



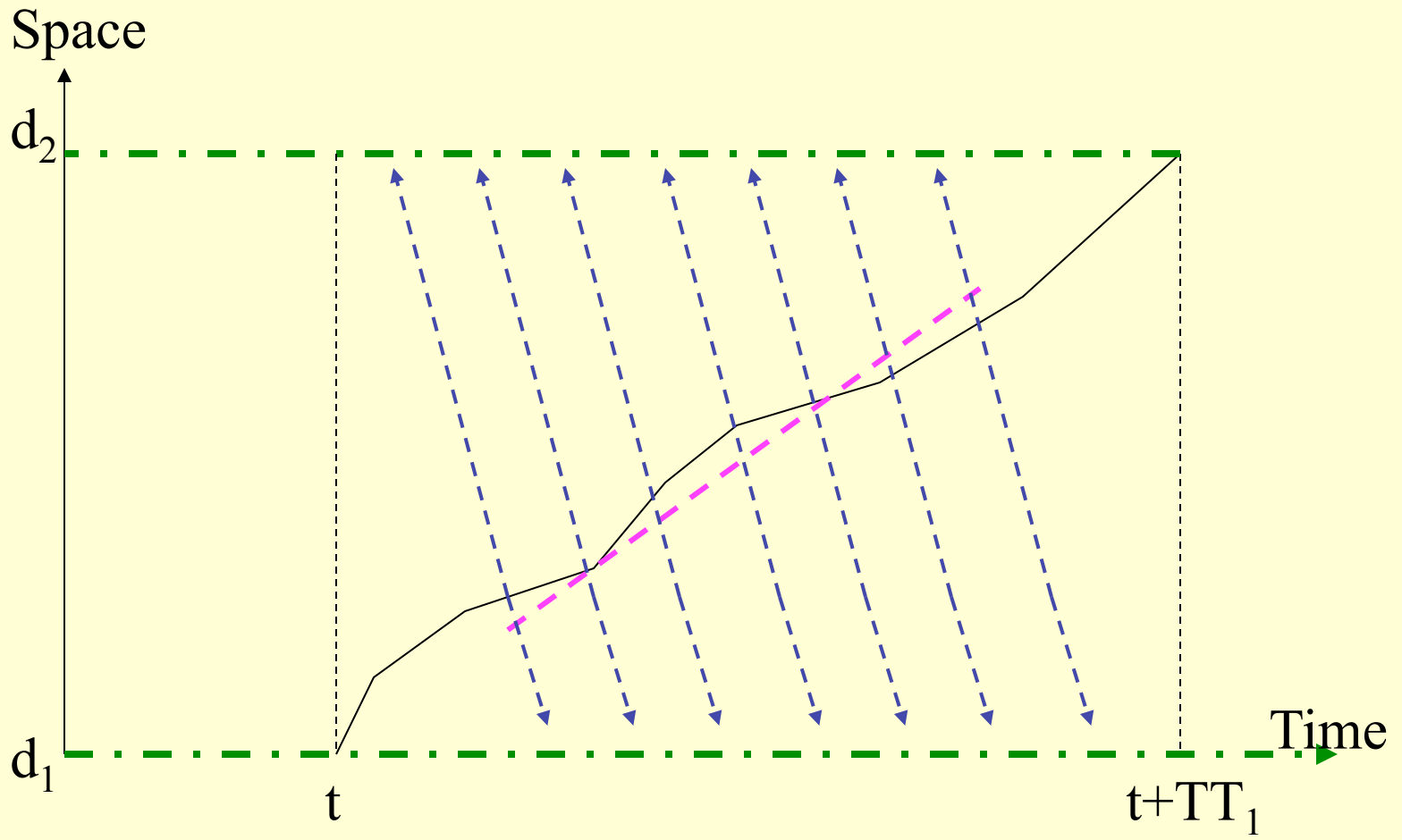


# An Enhanced Trajectory-based Method





# An Enhanced Trajectory-based Method





# Model Formulation

$$O(x, t) = \begin{cases} o_d \left( t + \frac{x - x_d}{u_c^{\max}}, t + \frac{x - x_d}{u_c^{\min}} \right) & , \text{ if } x - x_d < \hat{x} \\ o_{d+1} \left( t - \frac{x_{d+1} - x}{u_c^{\min}}, t - \frac{x_{d+1} - x}{u_c^{\max}} \right) & , \text{ if } x_{d+1} - x < \hat{x} \\ o_d \left( t + \frac{\hat{x} - x_d}{u_c^{\max}}, t + \frac{\hat{x} - x_d}{u_c^{\min}} \right) \\ + \frac{(x - x_d - \hat{x})}{\hat{x}} \\ \times \left( o_{d+1} \left( t - \frac{x - (x_{d+1} - \hat{x})}{u_c^{\min}}, t - \frac{x - (x_{d+1} - \hat{x})}{u_c^{\max}} \right) \right. \\ \left. - o_d \left( t + \frac{\hat{x}}{u_c^{\max}}, t + \frac{\hat{x}}{u_c^{\min}} \right) \right) & , \text{ otherwise} \end{cases}$$

$$\hat{x} = \begin{cases} \min\left(\frac{l_d}{3}, \frac{1}{3} \text{ mi}\right) & , \text{ when } l_d \geq 1 \text{ mile} \\ \frac{l_d}{3} & , \text{ otherwise} \end{cases} \quad x_d \leq x \leq x_{d+1}$$

$u_c^{\min}$  and  $u_c^{\max}$  are the minimum and the maximum traffic propagation speeds.





# Model Formation (cont'd)

$$u(x, t) = \begin{cases} u_{free} & , o(x, t) \leq o_{free} \\ u_{cong} + (u_{free} - u_{cong}) \left(1 - \frac{o(x, t) - o_{free}}{o_{cong} - o_{free}}\right)^m & , o_{free} < o(x, t) \leq o_{cong} \\ u_{min} + (u_{cong} - u_{min}) \left(1 - \frac{o(x, t) - o_{cong}}{o_{max} - o_{cong}}\right)^n & , o_{cong} < o(x, t) \leq o_{max} \\ u_{min} & , \text{otherwise} \end{cases}$$





# Travel Time Prediction

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- Parametric Models
  - Time series model
  - Linear regression model
  - Kalman Filter model
- Nonparametric models
  - Neural Network model
  - Nearest Neighbor model
  - Kernel model and local regression model





# Autoregressive Integrated Moving Average (ARIMA)

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- **Advantages:**

- Ability to predict a time series data set
- Good for predicting traffic data (volume, speed, or occupancy) at one detector

- **Disadvantages:**

- Focus on the mean value, therefore cannot well predict scenarios that less frequently occur
- It is hard to model multiple sets of time series data together (for example, multiple series of data from detectors)







# Linear Regression Models

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- One single linear regression model cannot predict well for all traffic scenarios, therefore multi-model structure is often used:
  - Layered/clustered linear regression model
  - Varying coefficient linear regression model





# Kalman Filter Model

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- Ability to auto-update parameters based on the evaluation of the prediction accuracy of the previous time interval
- Good performance when the true value can be obtained with a short delay (Chien et al., 2002 and 2003)
- May not work well for a prediction system with long travel times (long travel times = long delay for the update process)



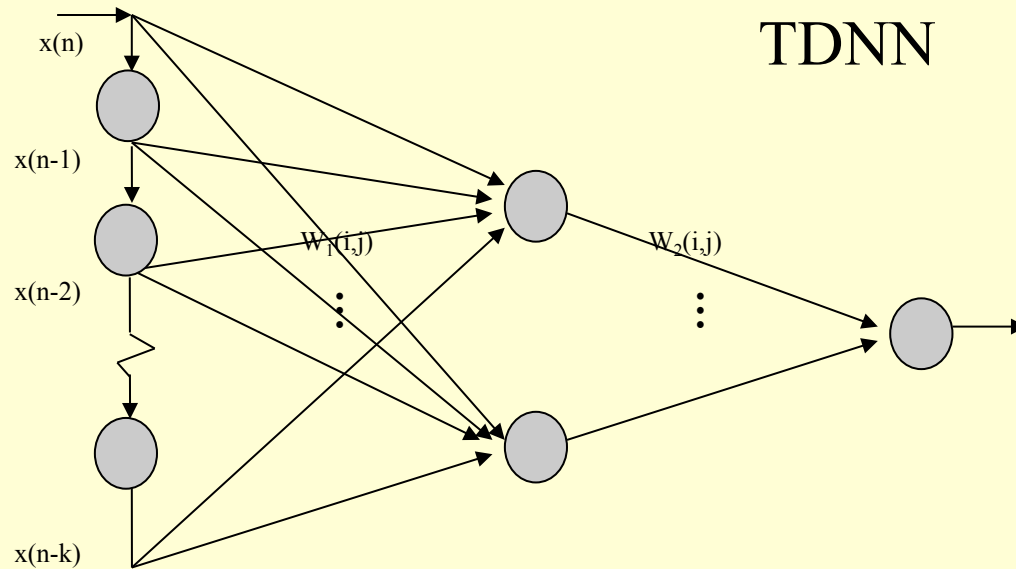
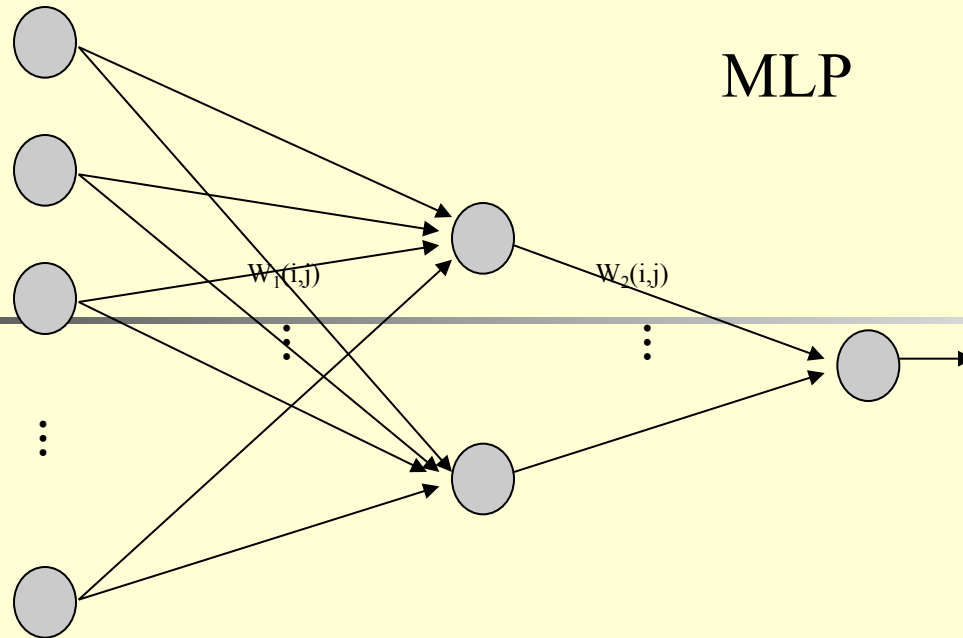


# Neural Network Models

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- Widely used to predict travel times
- Accurate and robust because of its good ability to recognize patterns
- Multi-layer Perceptron (MLP) and Time Delay Neural Network (TDNN) are mostly seen in the literature
- A large amount of training data







# *k*-Nearest Neighbor Model

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- Looks for *k* most similar cases as the current condition from the historical database to come out a prediction
- Requires a fairly large historical database

$$dist_{EUC}(p, q) = \sqrt{\sum_{i=1}^K (p_i - q_i)^2}$$

$$dist_{NUW}(p, q) = \sqrt{\sum_{i=1}^K w_i (p_i - q_i)^2}$$





# Other Nonparametric Models

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- Share a common structure
  - A clustering function
  - A kernel function (linear, nonlinear and/or other form) for each cluster
- For example
  - Kernel regression
  - Layered linear regression
  - Time-varying coefficient linear regression





# A Hybrid Travel Time Prediction Model

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- A  $k$ -Nearest Neighbor Model as the main model
  - For cases with sufficient good matches in the historical data
- An enhanced time-varying coefficient model as the supplemental model
  - For other cases





# *k*-Nearest Neighbor Model for Travel Time Prediction

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- An updated distance function
  - Based on three types of traffic state
- Geometric features
  - Take traffic data from critical lanes only
  - The time range of input data increases with the distance to the origin
- Daily and weekly traffic patterns
  - Varying search window based on historical traffic patterns







# Modified Definition of the Distance

$$mdis = \sqrt{\sum_{i=1}^k w_i (p_i^* - q_i^*)^2}$$

$$p_i^* = \begin{cases} p_i & , \text{ when } TC_d^{l_a}(t, t + \Delta t) = 0 \\ OC_d^{l_a} & , \text{ when } TC_d^{l_a}(t, t + \Delta t) = 1 \\ OF_d^{l_a} & , \text{ when } TC_d^{l_a}(t, t + \Delta t) = -1 \end{cases}$$

$$q_i^* = \begin{cases} q_i & , \text{ when } TC_d^{l_a}(t_h, t_h + \Delta t) = 0 \\ OC_d^{l_a} & , \text{ when } TC_d^{l_a}(t_h, t_h + \Delta t) = 1 \\ OF_d^{l_a} & , \text{ when } TC_d^{l_a}(t_h, t_h + \Delta t) = -1 \end{cases}$$





# Consideration of Traffic Patterns

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$$mdis = \sqrt{\sum_{i=1}^k w_i (\hat{p}_i - q_i^*)^2}$$

Where

$$\hat{p}_i = \begin{cases} M & , \text{if } |t - t_h| > T_{th}(d, t) \\ p_i^* \times \hat{w} & , \text{otherwise} \end{cases}$$

$$\hat{w} = \begin{cases} 1 & , \text{if } \exists s, wk_h \in \mathcal{W}_s \text{ and } wk_c \in \mathcal{W}_s \text{ (} 1 \leq s \leq S \text{)} \\ M & , \text{otherwise} \end{cases}$$

$$\bigcup_{s=1}^S \mathcal{W}_s = \{\text{all weekdays}\}$$

$M$  is a very large number.

$wk_c$  and  $wk_h$  are weekdays of the current case and the historical case respectively





# An Enhanced Time-varying Coefficient Model

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- Same global linear model structure
- Varying coefficients at each time interval
- A **linear relation** with time-varying coefficients between the **predicted travel time** and a *status travel time* (a preliminary prediction)





# Status Travel Time

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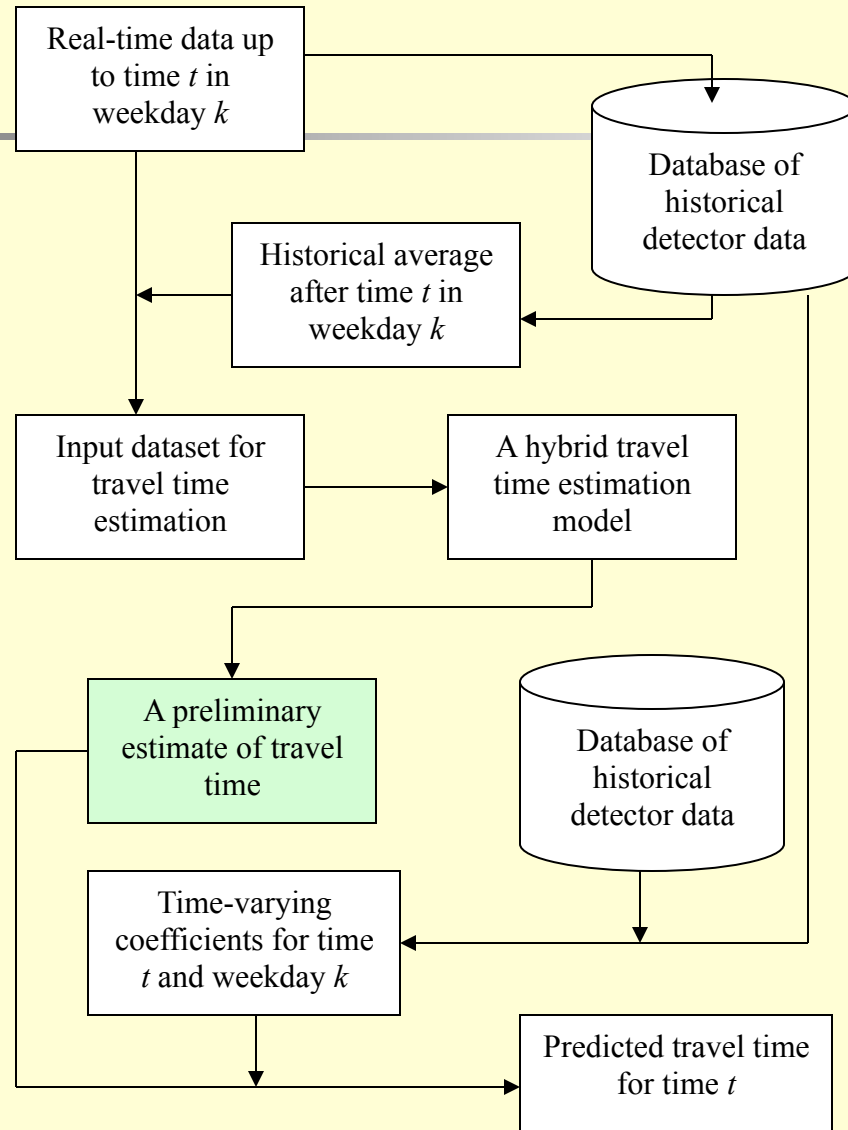
- Original form

$$T^*(t, \Delta) = \sum_{d=1}^{D-1} \frac{x_{d+1} - x_d}{v_d(t - \Delta)}$$





# Enhanced Status Travel Time for Long Links





# Model Formulation

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- Consider both daily and weekly traffic patterns

$$T(t) = a_{t_i}^k \hat{T}(t) + b_{t_i}^k$$

Where  $T(t)$  is the travel time to predict

$a_{t_i}^k$  and  $b_{t_i}^k$  are the weekly time varying coefficients for the  $t_i^{\text{th}}$  interval of the current weekday,  $k$ .





# Summary

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- Completed tasks
  - Perform an **in-depth review** of literature associated with travel time prediction
  - Develop a **modeling framework** for a travel time prediction system with sparsely distributed detectors on the freeway
  - Propose a hybrid model for **estimating travel times** for freeways with sparsely distributed detectors
  - Develop a hybrid model for **travel time prediction** for freeways with sparsely distributed detectors





# On-going Works

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- Incorporating a **Missing Data Estimation Module** to the Travel Time Prediction System
- Developing an Alternative Model Structure for Travel Time **Prediction** with **Neural Network** Models
- Developing an **Incident Detection Module** to Avoid Potential Large Errors under Non-recurrent Congestion
- Numerical Analysis with the Off-line Data for System Demonstration







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**Thank you!**

**Any questions?**

